

$$1) f(x) = -(x-6)^6 \quad x=5$$

$$f'(x) = -6(x-6)^5 \quad f'(5) = -6(5-6)^5 = -6(-1)^5 = 6$$

Угловой коэффициент касательной $m=6$

$$2) y = 3x^3 - 4x^2 + 3$$

$$y' = 9x^2 - 8x$$

$$9x^2 - 8x = 1$$

$$9x^2 - 8x - 1 = 0$$

$$x = \frac{8 \pm \sqrt{64 + 36}}{18}$$

$$x_1 = \frac{8+10}{18} = 1$$

$$x_2 = \frac{8-10}{18} = -\frac{1}{9}$$

$$3) y = \frac{2}{\sqrt{3}} \cos \frac{x}{2} - \sqrt{2} \quad x = 5\pi$$

$$y' = -\frac{2}{2\sqrt{3}} \sin \frac{x}{2}$$

$$\operatorname{tg} \alpha = -\frac{1}{\sqrt{3}} \sin \frac{\pi}{2} = -\frac{1}{\sqrt{3}}$$

$$\alpha = -\frac{\pi}{6} = -30^\circ = 150^\circ$$